

STT 200 – LECTURE 1, SECTION 2,4 RECITATION 4 (9/25/2012)

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Office hour: (C500 WH) 1:45 – 2:45PM Tuesday
(office tel.: 432-3342)

Help-room: (A102 WH) 11:20AM-12:30PM, Monday, Friday

Class meet on Tuesday:

3:00 – 3:50PM A122 WH, Section **02**

12:40 – 1:30PM A322 WH, Section **04**

OVERVIEW

- We will discuss following problems:
 - Chapter 6 “*The standard deviation as a rule and the normal model*” (Page 148): #16, 20, 28, 44, 46, 48
- All recitation PowerPoint slides available at [here](#)



- Chapter 6 (Page 148): #16:

Exam 1: Mean=80, Stdev=4, Reginald: 80 Sara: 88

Exam 2: Mean=70, Stdev=15, Reginald: 85 Sara: 65

- Explain Sara's point of view of deserving higher grade than Reginald.

- *Z scores: Reginald: 0, and 1, with total 1*

Sara: 2.0 and -0.33, with total 1.67

Sara has higher total Z-scores.



- Chapter 6 (Page 149): #20:

Mean=23.84, Stdev=3.56, speed limit=20 (mph)

- Speed limit 20 is how many Stdev from the mean?

$$(23.84 - 20) / 3.56$$

- Which observation is more unusual, 34 or 10?

$34 - 23.84 < 23.84 - 10$. So 10 is more distant from the mean 23.84 and hence more unusual.



- Chapter 6 (Page 149): #28:

Mean=100, Stdev=16

- Draw the normal model with 68-95-99.7 rule.
 - *We did in class.*
- Central 95% interval ($mean - 2stdev, mean + 2stdev$)
- % above 116 ($116 = mean + 1stdev$, so $(100 - 68) / 2$ %)
- % between 68 and 84 **$(95 - 68) / 2$ %, why?**
- % above 132 $(100 - 95) / 2$ %



- Chapter 6 (Page 151): #44:

N(100, 16)

- % over 80 *calculator: normcdf(80,100000,100,16)*
- % under 90 *calculator: normcdf(-100000, 90,100,16)*
- % between 112 and 132
 - *calculator: normcdf(112,132,100,16)*
 - *Note: use negative sign (-) instead of subtraction - !
Otherwise you will get syntax error.*



- Chapter 6 (Page 151): #46:

$N(100, 16)$, find cut-off value bound for

- the highest 5%

- *calculator: invNorm(0.95, 100,16)*

- the lowest 30%

- *calculator: invNorm(0.3, 100,16)*

- the middle 80%

- *calculator: invNorm(0.1, 100,16)*

- *calculator: invNorm(0.9, 100,16)*



- Chapter 6 (Page 152): #48:

All IQ's follows $N(100, 16)$,

- what IQ represents the 15th percentile?

- *calculator: $invNorm(0.15, 100, 16)$*

- what IQ represents the 98th percentile?

- *calculator: $invNorm(0.98, 100, 16)$*

- the IQR?

- *$invNorm(0.75, 100, 16) - invNorm(0.25, 100, 16)$*



○ Summary

- *Z-score follows standard normal distribution (mean=0, stdev=1). To compare over multiple normal distributions, we can standardize the data and use the Z-score.*
- *Learn 68-95-99.7 rule and the fact that Normal distribution is symmetric!*
- *Given quantile, find percentile: normcdf(lower bound, upper bound, mean, stdev)*
- *Given percentile, find quantile: invNorm(percentile, mean, stdev)*
- *Percentile is defined in left-tail (or lower tail)*
- *Percentile is a number from 0 to 1(or 0% to 100%). Quantile can be any number, usually of same order of magnitude as the normal mean.*

