

Here is the list of exam 2 scores arranged by size.

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in[246]:= exam2scores = {0, 0, 0, 0, 4, 5, 5, 6, 6, 6, 6, 6, 6, 6, 7, 7, 7, 8, 8, 8, 8, 8,  
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12, 12, 12, 12, 12, 12, 13, 13, 13, 13, 13, 13, 14, 14, 14, 14, 14, 14,  
14, 15, 15, 15, 15, 15, 15, 15, 15, 15, 16, 16, 16, 16, 16, 16,  
16, 16, 17, 17, 17, 17, 17, 17, 17, 18, 18, 18, 18, 18, 18, 18,  
18, 18, 18, 19, 19, 19, 19, 19, 19, 19, 19, 19, 19, 19, 19, 20, 20}
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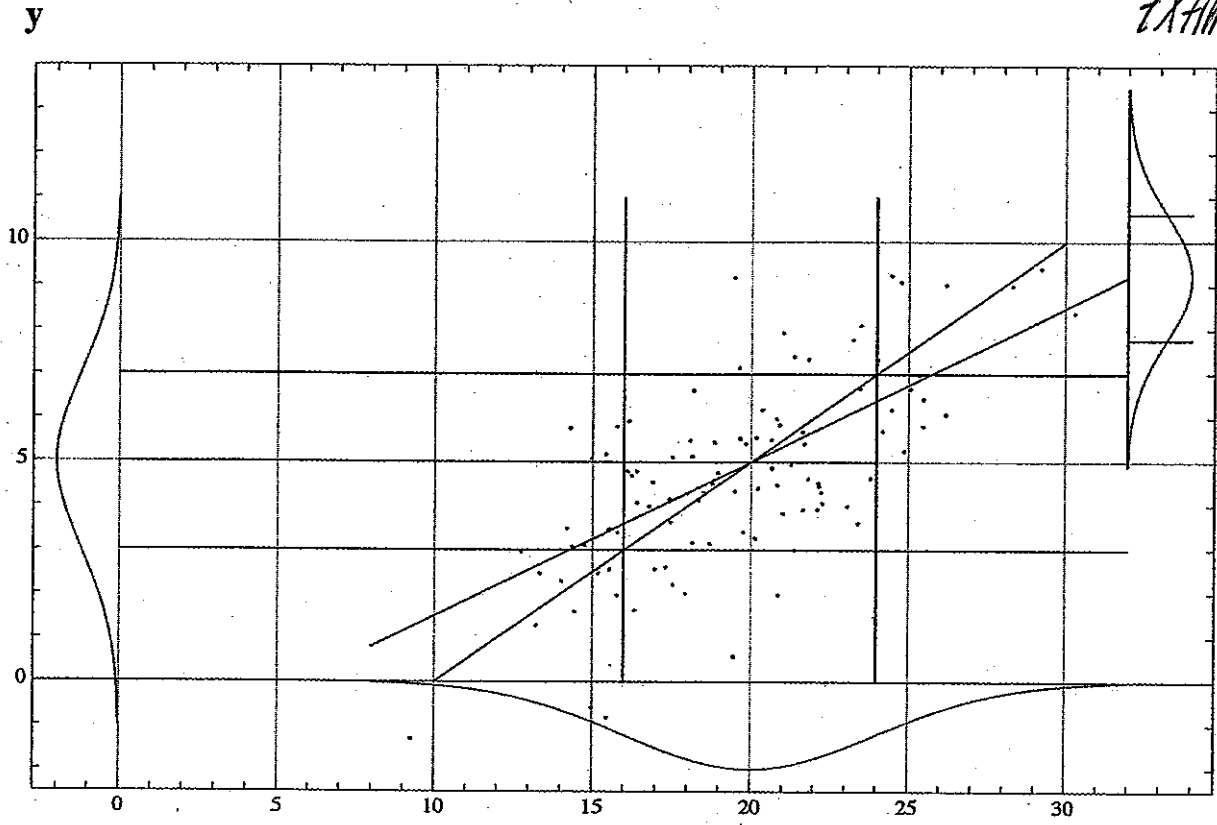
Your raw score (number correct) on exam 2 will be the last score in the scores reported to you by the registrar in a mailing that should come to you later today.

Here is the formula for converting your raw score into a GRADE.

$$\text{exam 2 GRADE} = 2.0 + 0.4 (\text{exam 2 raw score} - 12)$$

Questions 1 through 4 refer to the figure below. The distribution of  $(x, y)$  is 2 - dimensional normal (bi - variate normal) vaguely represented by a modest - sized sample of points  $(x, y)$ . All curves plotted are for the population not for the sample.

EXAM 2



1. Determine the *population correlation*  $R$  of  $x, y$ .

- a) 0.88   b) 0.70   c) 0.45   d) 0.54   e) 0.99

ITEM	1	TEST 7300	09 10 15	X			
	1	2*	3	4	5	OMT NO	105
U	7	68	11	14	0	0	DIFF 51
L	18	21	18	21	21	0	DISC 46

2. Determine the *population standard deviation*  $\sigma_y$  of  $y$ .

- a) 2   b) 5   c) 4   d) 1   e) 3

ITEM	2	TEST 7300	09 10 15				
	1*	2	3	4	5	OMT NO	105
U	89	4	4	4	0	0	DIFF 32
L	25	43	14	4	14	0	DISC 64

3. Use the regression line to *predict*  $y$  conditional on  $x = 32$  (choose closest answer)

- a) 7   b) 8   c) 6   d) 5   e) 9

ITEM	3	TEST 7300	09 10 15				
	1	2	3	4	5*	OMT NO	105
U	0	0	0	0	100	0	DIFF 5
L	0	14	0	0	86	0	DISC 14

4. Determine standard deviation of *error of prediction* at  $x = 20$  (not a typo).

- a) 3.4   b) 4.4   c) 1.4   d) 2.4   e) 0.4   (choose closest answer)

ITEM	4	TEST 7300	09 10 15				
	1	2	3*	4	5	OMT NO	105
U	0	4	93	0	4	0	DIFF 55
L	14	32	25	11	18	0	DISC 68

Questions 5-8 assume that score  $x$  in a particular population is distributed as normal with mean 10 and standard deviation 4.

5. Determine the standard score  $z$  of a person having  $x$  score 15.

- a) 1.46   b) 0.9   c) 0.2   d) 1.25   e) 0.75

ITEM	5	TEST	7300	09	10	15
	1	2	3	4*	5	OMT NO 105
U	0	0	0	100	0	0 DIFF 11
L	11	11	7	61	11	0 DISC 39

6. Determine  $P(x < 15)$  (choose nearest answer).

- a) 0.94   b) 0.52   c) 0.89   d) 0.97   e) 0.63

ITEM	6	TEST	7300	09	10	15
	1	2	3*	4	5	OMT NO 105
U	0	0	100	0	0	0 DIFF 11
L	11	4	64	14	7	0 DISC 36

7. Find the 90th percentile of *standard normal*  $z$  (use closest table entry).

- a) 1.28   b) 1.04   c) 0.86   d) 0.71   e) 0.53

ITEM	7	TEST	7300	09	10	15
	1*	2	3	4	5	OMT NO 105
U	100	0	0	0	0	0 DIFF 25
L	32	14	29	11	14	0 DISC 68

8. Using #7 find the 90th percentile of  $x$ .

- a) 10.61   b) 13.03   c) 15.12   d) 11.71   e) 9.92

ITEM	8	TEST	7300	09	10	15
	1	2	3*	4	5	OMT NO 105
U	0	4	96	0	0	0 DIFF 31
L	11	29	21	29	7	4 DISC 75

Questions 9 through 11 deal with algebraic properties of sample mean, sample standard deviation and correlation.

9. If sample mean of a list  $y$  is 5 what is the sample mean of list  $3x - 2$ ?

- a) 13   b) 15   c) 3   d) 1   e) 10

ITEM	9	TEST	7300	09	10	15
	1*	2	3	4	5	OMT NO 105
U	89	11	0	0	0	0 DIFF 13
L	71	14	0	11	4	0 DISC 18

10. If  $s_x$  (of list  $x$ ) is equal to 2 what is the *sample standard deviation* of the list  $3x + 4$ ?

- a) 2   b) 0.33   c) 8   d) 10   e) 6

ITEM	10	TEST	7300	09	10	15
	1	2	3	4	5*OMT	NO 105
U	0	0	0	7	93	0 DIFF 39
L	54	0	4	29	14	0 DISC 79

11. If correlation between  $(x, y)$  is 0.3 what is the correlation between  $(x+4, 3y+2)$ ?

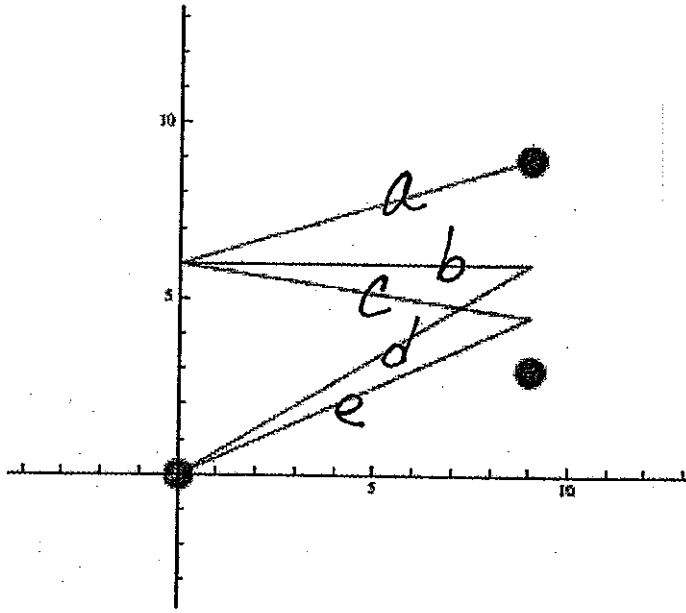
- a) 0.9   b) 4.9   c) 0.6   d) 0.3   e) none of the others

ITEM	11	TEST	7300	09	10	15
	1	2	3	4*	5	OMT NO 105
U	0	0	0	100	0	0 DIFF 10
L	7	0	11	71	11	0 DISC 29

Questions 12 through 15 are about calculations of means, standard deviations, correlation in relation to the following data of (x, y) pairs (column means are recorded at the bottom):

x	y	x <sup>2</sup>	y <sup>2</sup>	xy
0	0	0	0	0
9	3	81	9	27
9	9	81	81	81
-	-	-	-	-
6.	4.	54.	30.	36.

12. Which of the five lines is the regression line?



ITEM	12	TEST	7300	09	10	15
	1	2	3	4*	5	OMT NO 105
U	0	4	0	89	7	0 DIFF 35
L	14	0	7	54	25	0 DISC 36

13. Is the least squares line for this data the same as the regression line?

- a) Yes    b) No

ITEM	13	TEST	7300	09	10	15
	1*	2	3	4	5	OMT NO 105
U	89	11	0	0	0	0 DIFF 30
L	50	50	0	0	0	0 DISC 39

14. Calculate the sample standard deviation  $S_x$ .

- a) 3.812    b) 2.798    c) 1.638    d) 5.196    e) 3.894

ITEM	14	TEST	7300	09	10	15
	1	2	3	4*	5	OMT NO 105
U	4	0	4	93	0	0 DIFF 37
L	14	7	21	29	29	0 DISC 64

15. Calculate the correlation R for the sample data.

- a) 0.58    b) 0.76    c) 0.47    d) 0.69    e) 0.61

ITEM	15	TEST	7300	09	10	15
	1	2*	3	4	5	OMT NO 105
U	0	100	0	0	0	0 DIFF 41
L	25	18	29	25	4	0 DISC 82

Questions 16 through 20 concern T and z based confidence intervals and the margin of error. Unless specified in a problem, the population scores are "not assumed" to be normal distributed. Suppose with-replacement equal-probability sampling and

$$\bar{x} = 48 \quad s_x = 6 \quad n = 70 \quad N = 800.$$

16. Give the estimated margin of error for the sample mean.

- a) 1.1   b) 1.6   c) 1.5   d) 1.4   e) 1.2

ITEM	16	TEST	7300	09	10	15
	1	2	3	4*	5	OMT NO 105
U	0	0	0	100	0	0 DIFF 31
L	4	18	32	36	11	0 DISC 64

17. Give the right endpoint of the 95% confidence interval for  $\mu_x$  based on this data (choose the closest value).

- a) 49.1   b) 49.2   c) 49.3   d) 49.4   e) 49.5

ITEM	17	TEST	7300	09	10	15
	1	2	3	4*	5	OMT NO 105
U	0	4	0	96	0	0 DIFF 47
L	18	29	21	18	14	0 DISC 79

18. If instead of sampling with-replacement we sampled without-replacement what would be the right endpoint of the 95% confidence interval for  $\mu_x$  based on this data (choose the closest value)?

- a) 49.10   b) 49.21   c) 49.34   d) 49.46   e) 49.58

ITEM	18	TEST	7300	09	10	15
	1	2	3*	4	5	OMT NO 105
U	4	21	68	7	0	0 DIFF 54
L	14	18	18	32	18	0 DISC 50

19. If instead we had this same data but from a sample of only  $n = 10$  and if the population distribution is known to be close to normal (making N essentially infinite) what number would we use in place of the z-score when calculating a 95% confidence interval for  $\mu_x$ ?

- a) 2.63   b) 2.87   c) 3.05   d) 2.26   e) 2.48

ITEM	19	TEST	7300	09	10	15
	1	2	3	4*	5	OMT NO 105
U	0	4	0	96	0	0 DIFF 36
L	25	11	14	32	18	0 DISC 64

20. If the data above refer to a sample of  $n = 10$  from a normal population give the right endpoint of a 95% confidence interval for the population mean.

- a) 61.6   b) 49.4   c) 52.3   d) 62.9   e) 58.4

ITEM	20	TEST	7300	09	10	15
	1	2	3*	4	5	OMT NO 105
U	0	7	86	4	4	0 DIFF 51
L	29	25	29	14	0	4 DISC 57