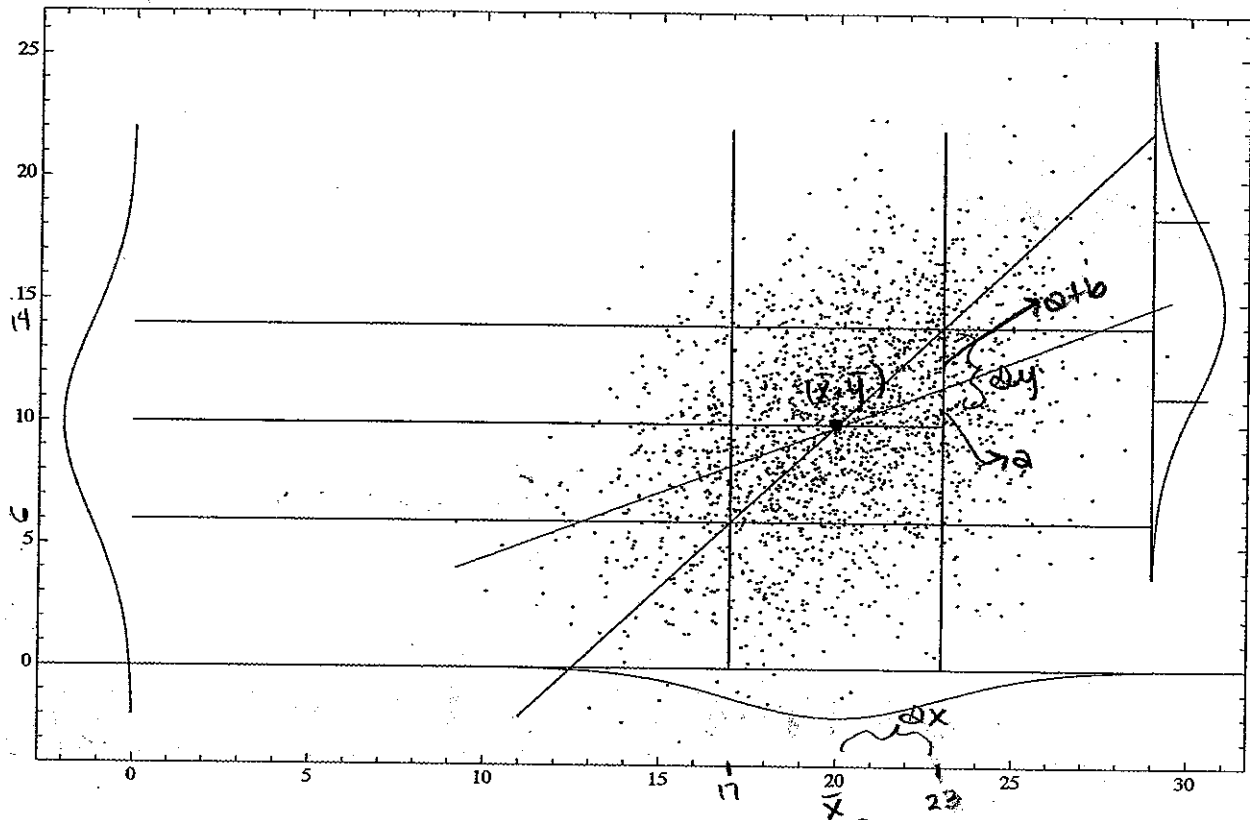


1 - 7. Refer to the (x, y) plot below (y is vertical).  
 Closest answers. Pay attention to scales on axes and origin.



1.  $\mu_x$  (approx  $\bar{x}$ ) (a) 17 (b) 18 (c) 19 (d) 20 (e) 21
2.  $S_x$  (a) 1 (b) 2 (c) 3 (d) 4 (e) 5  $= \frac{23-17}{2} = 3$
3.  $S_y$  (a) 2 (b) 3 (c) 4 (d) 5 (e) 6  $= \frac{14-6}{2} = 8/2 = 4$
4.  $r$  (a) 1 (b) .75 (c) .4 (d) .0  $r = a/(cb) = 1.5/4 = .375$
5. sd of y for  $x = 15$  (a) 0 (b) 1.6 (c) 2.9 (d) 3.5

$$\text{std. dev.} = \sqrt{1-r^2} (S_y) = \sqrt{1-(.4)^2} (4) = 3.6666$$

6. naive line slope (a) 1.3 (b) 2.1 (c) 3.0 (d) 3.6 (e) 4.5

$$\text{naive slope} = \Delta y / \Delta x = 4/3 = 1.33$$

7. regrline slope (a) .2 (b) .5 (c) .7 (d) 1.1 (e) 1.5

$$\text{regr. slope} = r (\Delta y / \Delta x) = .4 (1.3) = .52$$

8-12. For the data whose averages are reported below, choose closest answers.

x	y	x <sup>2</sup>	y <sup>2</sup>	xy
1	0	1	0	0
2	8	4	64	16
3	10	9	100	30
6	6	36	36	36
$\bar{x}$	$\bar{y}$	$\bar{x^2}$	$\bar{y^2}$	$\bar{xy}$
3.	6.	12.5	50.	20.5

$$\hat{\sigma}_x = \sqrt{12.5 - (3^2)}$$

8.  $s_x$  (a) 1 (b) 2 (c) 3 (d) 4 (e) 5

$$\hat{\sigma}_x = \sqrt{x^2 - \bar{x}^2} = \sqrt{12.5 - (3^2)} = 1.87$$

9.  $s_y$  (a) 1.7 (b) 2.7 (c) 3.7 (d) 4.7 (e) 5.7

$$\hat{\sigma}_y = \sqrt{y^2 - \bar{y}^2} = \sqrt{50 - (6^2)} = 3.74$$

$$20.5 - 18 = \frac{2.5}{0.919} = 3.6$$

10.  $r$  (a) .26 (b) .36 (c) .46 (d) .56 (e) .66

$$r = \frac{\bar{xy} - \bar{x}\bar{y}}{\sqrt{x^2 - \bar{x}^2} \sqrt{y^2 - \bar{y}^2}} = \frac{20.5 - (3 \cdot 6)}{(1.87)(3.7)} =$$

11. naive line slope (a) 0 (b) 1 (c) 2 (d) 3 (e) 4

$$\text{naive slope} = \frac{dy}{dx} = 3.7 / 1.87 = 1.97$$

12. regr line slope (a) .6 (b) .7 (c) .8 (d) .9 (e) 1

$$\text{regr. slope} = r \left( \frac{dy}{dx} \right) = .36 (1.97) = .7092$$

13-15. A multiple linear regression on males at risk for stroke employs variables  
 $y$  = probability of stroke within five years  
 $x_1$  = age (years)                       $x_2$  = years since last incident

The MLR gives  $R = 0.86$ ,  $S_y = 0.07$ ,  $\hat{b}_0 = 0.17$ ,  $\hat{b}_1 = 0.003$ ,  $\hat{b}_2 = -0.02$ .

13. Fraction of  $S_y$  explained by MLR. (a) .70 (b) .74 (c) .78 (d) .82 (e) .86

$$R = 0.86 \rightarrow R^2 = 0.86^2 = .7396$$

14.  $\hat{y}$  (predicted probability of a stroke within five years) for a subject 74 yrs of age, with 5 years since his last incident.

(a) 0.07 (b) 0.14 (c) 0.29 (d) 0.33 (e) 0.36

$$\hat{y} = \hat{b}_0 + \hat{b}_1 x_1 + \hat{b}_2 x_2 \quad \hat{y} = 0.17 + 0.003(74) + -0.02(5)$$

$$\hat{y} = .292$$

15. If the multidimensional plot is normal (elliptical) what is the standard deviation of  $y$  for all subjects 74 years of age with 5 years since their last incident?

(a) .006 (b) .036 (c) .066 (d) .096 (e) .126

$$\sqrt{1-r^2} (S_y) = \sqrt{1-.74} (.07) = .0356$$

16-19 These concern MLR and straight line regression in general.

16. What is the range of  $R$  in general? (a)  $[0, 1]$  (b)  $[-1, 1]$  (c)  $[-0.5, 0.5]$

17. If in a MLR we have  $r[y, \hat{y}] = 0.7$  what is  $R$ ?

(a) 0.49 (b) 0.7 (c)  $1 - 0.49$  (d)  $1 - 0.7$

$$r_{MLR} = |r| \quad r[y, \hat{y}] = 0.7$$

$$r[x, \hat{x}]$$

18. For straight line regression what is  $r[-3x+4, 2y-6]$ ?

(a)  $-6 r[x, y]$  (b)  $-6 r[x, y] - 24$  (c)  $r[x, y]$  (d)  $r[x, y]$  (e)  $r[x, y] - 24$

$$r[-3/x + 4, 2y - 6] = -r[x, y]$$

19. If in a straight line regression we have  $r[x, y] = -0.5$  what is  $R$ ?

(a) -0.5 (b) -0.25 (c) 0.25 (d) 0.5 (e) .75

$$b_i c \quad r_{MLR} = |r|$$

