

“90 subjects diagnosed for depression enlisted for comparison of treatments for depression. Subjects were randomly divided into three groups 30 ea and given pills to take over 3 months.”
 Desired to test H0: rate of return to depression same for all three types of pill vs H1: not all same.

STAT 200 4-27-09a

observed table

	Placebo	Saint John's wort	Posrex	
Depression returned	24	22	14	60
No sign of depression	6	8	16	30
fixed totals	30	30	30	90

H0: RATE DEPR SAME FOR ALL 3 GROUPS H1: NOT ALL SAME

“expected” table under H0

	Placebo	Saint John's wort	Posrex	
Depression returned	30 * 60 / 90 = 20	30 * 60 / 90 = 20	20	60
No sign of depression	10	10	10	30
fixed totals	30	30	30	90

Chi square statistic = $\frac{(24 - 30 \cdot 60 / 90)^2}{(30 \cdot 60 / 90)} + \dots = 0.8 + 0.2 + 1.8 + 1.6 + 0.4 = 3.6^*$
 = 8.4 ✓ with df = (R-1)(C-1) = (2-1)(3-1) = 2.

P-value = Pr(chi square with 2 df > 8.4) = 0.015.

0.025 0.01
 2 df 7.378 (8.4 is in between) 9.210 so P-value is between 0.025 and 0.01.

NOTE: LOOK AT $(16 - 10) / \sqrt{10}$ POSITIVE “LARGE”

THIS 3.6 LARGE
 CONTRIB OF “NO SIGN POSREX”

Binomial: p = probability of "success," $q = 1-p$.

- CH 19 RECALL -

17-21. IF more than 20% of emergency responders require additional training THEN additional money will have to be found.

17. Suggest H_0 and H_1 for a z-test to address the issue.

If set it up $H_0: p = 0.2$ NEED TRAINING

$H_1: p > 0.2$ " "

AND CONTROL $\alpha = P(\text{REJ } H_0 \mid H_0 \text{ IS TRUE})$

eg If we can live w/ a ^{WHEN} 10% chance of REJ H_0 when it is true (i.e. FALSE POSITIVE)

ORDINARY TERMS: IF $p \leq 0.2$ ($p = 0.2$ STANDS IN)

THE WE'LL HAVE 10% OF MAKING MISTAKE OF REJ H_0 .

How? TAKE SAMPLE. CALC χ^2 STAT, DF, P-VALUE.

If P-VALUE ≤ 0.10 then REJECT H_0

How to
USE P-VALUE
to TEST w/
 $\alpha = 0.10$

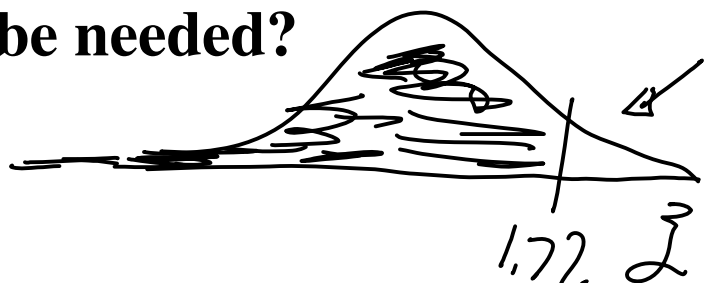
18. A random sample of 200 emergency responders finds 50 who require the training. Calculate an appropriate z-test statistic.

$\hat{p} = \frac{50}{200} = .25$
 $\chi^2_{STAT} = 1.77$
 $(Z\text{-TEST})_{STAT} = \frac{\hat{p} - p_0}{\sqrt{p_0 q_0 / n}} = \frac{.25 - .2}{\sqrt{.2 \cdot .8 / 200}}$

$p_0 = .2$ $q_0 = .8$

ALL ABOUT p

19. Determine the P-value. Does it seem that additional money will be needed?



P-VALUE SINCE $H_1: p > .2$ { EVIDENCE AGAINST H_0 IS TO RIGHT }

$z = 1.7$

$P(Z < z) = 0.9616$

ans. P-value $\sim P(Z > 1.77) = 1 - 0.9616 = 0.0384$.

NOT HIGHLY SIGNIFICANT .04 NOT ALL THAT SMALL. OBS SIG LEVEL

20. If instead $H_1: "p \text{ is not } .2"$ is this a one-sided or two-sided test?

$H_1: .2$

2-SIDED TEST SINCE H_1 FALLS BOTH SIDES OF H_0 .

21. For $H_1: "p \text{ is not } .2"$ determine the P-value from (19).

ans. $2(0.0384) = 0.0768$



22. For a test of $H_0: p = 0.2$ versus $H_1: "p \text{ is not } 0.2"$ we may employ chi square goodness of fit. Give the table of exp and obs counts for such a test if a sample of 200 finds 50 (as above).

	require training	do not require training	$H_0: p = 0.2$
exp	$.2 \cdot 200 = 40$	160	200
obs	50	150	200

$H_1: p \neq 0.2$

std score

$$DF = C - 1 = 2 - 1 = 1$$

23. Refer to (22). Determine the chi square statistic for the test.

$$\sum_{2 \text{ CELLS}} \frac{(obs - exp)^2}{exp} = \frac{(50 - 40)^2}{40} + \frac{(150 - 160)^2}{160} = 3.125$$

24. Refer to (22). Determine the P-value.

$$\Pr(\text{chi square } 1 \text{ df} > 3.125) \sim \underline{.0771} \quad \text{COMPUTER.}$$

DF	.10		.05	CLOSE
1	2.71	<u>3.125</u>	3.84	

Compare P-value with that of two-sided z-test (which was 0.0768).

25. Meta Analysis. Each of two experimenters independently finds

$$\text{chi sq} = 9.54 \quad \text{df} = 6$$

$$\text{chi sq} = 14.33 \quad \text{df} = 9$$

Test H0: both null hypotheses are correct.

~~_____~~
H0: BOTH EXP 1
EXP 2
HAVE CORRECT MODEL.

Y G B R 50%
.38 .1 .06 REST

MA M
S, P

$$\chi^2 \text{ TEST} \quad \text{DF} = 4 - 1 = 3,$$

SOME exp POSSIBLY < 5 RULE OF THUMB.

$$\chi^2 \text{ STAT} = 9.54 + 14.33$$

$$\text{DF} = 6 + 9 = 15$$

+ MAYBE GET exp ≥ 5

IN ALL CELLS.

WORKS SINCE χ^2 (FIRST) = DIST $Z_1^2 + \dots + Z_6^2$ UNDER
 χ^2 (SECOND) = " $Z_1^2 + \dots + Z_9^2$