

$P(A \cup B) = P(A) + P(B) - P(A \cap B)$ addition rule

$P(A \cap B) = P(A) P(B | A)$ multiplication rule

$P(B | A) = P(A \cap B) / P(A)$ variant of above

$P(B | A) = P(B)$ is equivalent to A independent of B

$P(A \cap B) = P(A) P(B)$ is equivalent to A independent of B

$\mu_X = E X = \sum_x x p(x)$ expectation, or mean, of r.v. X
 $= \int x f(x) dx$ expectation in continuous case

$\sigma_X = \sqrt{E (X - E X)^2}$ standard deviation of r.v. X
 $= \sqrt{E X^2 - (E X)^2}$ another way to calculate it

$E (a X + b Y + c) = a E X + b E Y + c$ for r.v. X, Y

constants a, b, c

$E (X Y) = (E X) E(Y)$ if r.v. X, Y are independent

$\sigma_{X+Y} = \sqrt{\sigma_X^2 + \sigma_Y^2}$ for independent r.v. X, Y

$\sigma_{aX+b} = |a| \sigma_X$ in particular $\sigma_X = \sigma_{-X}$

$\sigma_{\bar{X}} = \frac{\sigma_X}{\sqrt{n}}$ \bar{X} = the average of n independent r.v. X_i
 each having the distribution of r.v. X

$$\sigma_{\bar{X}} = \sqrt{\frac{N-n}{N-1}} \frac{\sigma_X}{\sqrt{n}} \quad \text{when the samples are without replacement from a population of size } N$$

$$E \bar{X} = E X \quad \text{in each of the above two cases}$$

Central Limit Theorem (CLT): The distribution of \bar{X} is approximately normal (bell) in both cases above.