

**TO START THIS MATHEMATICA NOTEBOOK YOU CLICK ITS FILENAME.**

**You will have to use a computer in a university lab (e.g. Wells Hall B-Wing)**

This *Mathematica* notebook contains a number of useful functions described in the handout and briefly indicated below. The first time you attempt to use one of these functions a panel will pop up asking "Do you want to evaluate all the initialization cells?" to which you must answer yes.

To enter a given command line you click on the screen whereupon a horizontal line should appear at the cursor. When right brackets are in view on the *Mathematica* panel you want to click at a place where a horizontal line will extend between two such brackets if you desire a new line. If you attempt to type multiple commands into a single bracketed location *Mathematica* will become confused.

Type the command you wish to execute then PRESS THE ENTER KEY ON THE NUMERIC KEYPAD. This is required because *Mathematica* wants to use the return or other enter key to move to the next line. You do not want to move to a new line. You want to enter a command. That is why you must use the ENTER key on the numeric keypad.

To save your work select save from the pull down file menu, which saves it as a *Mathematica* .nb (notebook) file. If you wish to print your work at home select print then the option of saving as a PDF. You will be unable to work with the .nb *Mathematica* file itself unless you have *Mathematica* installed (unlikely) but you can transport and print the .pdf file virtually anywhere.

**Click the line below and press ENTER on the numeric keypad.**

```
size[{4.5, 7.1, 7.8, 9.1}]
```

4

Just above, I clicked to open a new line then typed

```
size[{4.5, 7.1, 7.8, 9.1}]
```

followed by a press of the numeric keypad ENTER key. Notice that off to the right of the entry there are nested brackets joining the command line and its output 4 = the number of data items in {4.5, 7.1, 7.8, 9.1}.

## ■ A complete list of the commands in this notebook and what they do.

**size**{4.5, 7.1, 7.8, 9.1} returns 4

**mean**{4.5, 7.1, 7.8, 9.1} returns the mean 7.125

**median**{4.5, 7.1, 7.8, 9.1} returns the median of the list {4.5, 7.1, 7.8, 9.1}

**s**{4.5, 7.1, 7.8, 9.1} returns the sample standard deviation  $s=1.93628$

**sd**{4.5, 7.1, 7.8, 9.1} returns the n-divisor version of standard deviation  $s=1.67686$

**r**[**x**, **y**] returns the sample correlation  $r = \frac{\overline{xy} - \bar{x}\bar{y}}{\sqrt{\overline{x^2} - \bar{x}^2} \sqrt{\overline{y^2} - \bar{y}^2}}$  for paired data.

**sample**{4.5, 7.1, 7.8, 9.1}, 10] returns 10 samples from {4.5, 7.1, 7.8, 9.1}

**ci**{4.5, 7.1, 7.8, 9.1}, 1.96] returns a 1.96 coefficient CI for the mean from given data

**bootci**[mean, {4.5, 7.1, 7.8, 9.1}, 10000, 0.95] returns 0.95 bootstrap ci for pop mean

**smooth**{4.5, 7.1, 7.8, 9.1}, 0.2] returns the density for data at bandwidth 0.2

**smooth2**{4.5, 7.1, 7.8, 9.1}, 0.2] returns the density for data at bandwidth 0.2

overlaid with normal densities having  $sd = 0.2$  around each data value

**smoothdistribution**{1, 700}, {4, 300}, 0.2] returns the density at bandwidth 0.2

for a list consisting of 700 ones and 300 fours.

**popSALES** is a file of 4000 sales amounts used for examples

entering `popSALES` will spill 4000 numbers onto the screen. To prevent that enter `popSALES;` instead (the appended semi-colon suppresses output).

**betahat**[**matrix x**, **data y**] returns the least squares coefficients  $\hat{\beta}$  for a fit of the model  $y = x\beta + \epsilon$ .

**resid**[**matrix x**, **data y**] returns the estimated errors  $\hat{\epsilon} = y - x\hat{\beta}$  (see **betahat** above).

**R**[**matrix x**, **data y**] returns the **multiple correlation** between the fitted values  $x\hat{\beta}$  and data **y**.

```
Mean [popSALES]
```

```
14.8951
```

```
sd [popSALES]
```

```
9.34
```

The next line finds a sample of 40 from popSALES. The line below that finds a 95% z-CI for the population mean. It outputs {mean, n, s, z (or t), CI}.

In *Mathematica* the percent character % refers to the output of the very last command execution.

```
mysample = sample [popSALES, 40];
```

```
ci [mysample, 1.96]
```

```
{13.8223, 40., 8.81266, 1.96, {11.0912, 16.5533}}
```

```
bootci[mean, mysample, 10000, 0.95]
```

```
( Confidence Level      0.95  
  Estimator            mean  
  Estimate             13.8223  
  Sample Size         40  
  bs Replications #1  10000  
  bootstrap C ci Half Width 2.68175  
  CI                  {11.1405, 16.504} )
```

```
median[popSALES]
```

```
12.61
```

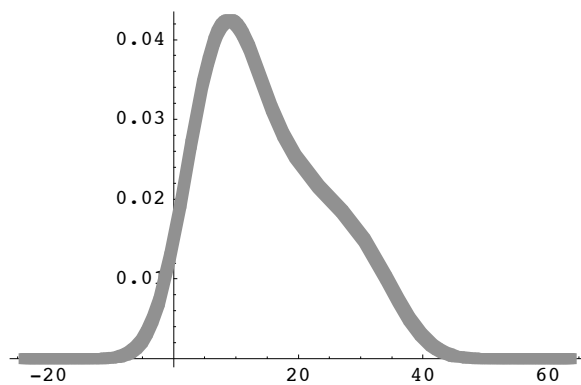
```
median[mysample]
```

```
13.395
```

```
bootci[median, mysample, 10000, 0.95]
```

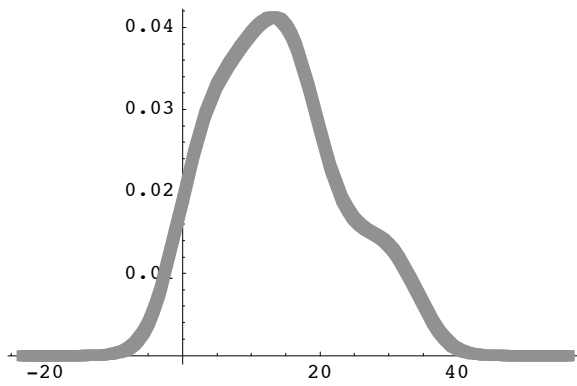
```
( Confidence Level      0.95  
  Estimator            median  
  Estimate             13.395  
  Sample Size         40  
  bs Replications #1  10000  
  bootstrap C ci Half Width 3.315  
  CI                  {10.08, 16.71} )
```

```
smooth[popSALES, 4]
```



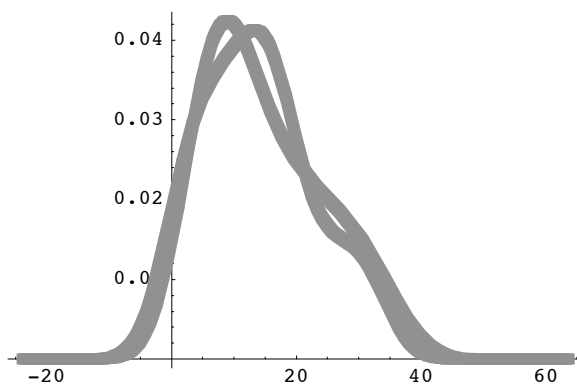
```
- Graphics -
```

```
smooth[mysample, 4]
```



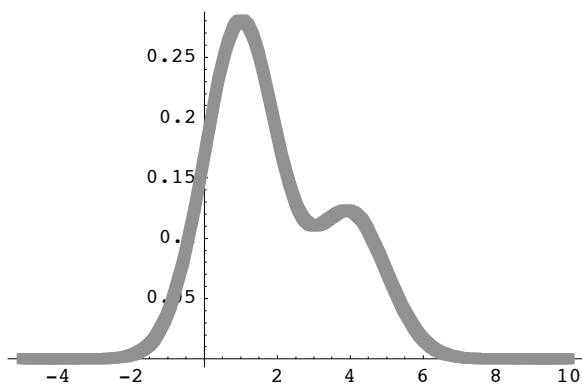
```
- Graphics -
```

```
Show[%, %%]
```



```
- Graphics -
```

```
smoothdistribution[{{1, 700}, {4, 300}}, 1]
```



```
- Graphics -
```

Reproducing the curves of Figure 7.13 produced by smoothing data  
 $\{84, 49, 61, 40, 83, 67, 45, 66, 70, 69, 80, 58, 68, 60, 67, 72, 73, 70, 57, 63, 70, 78, 52, 67, 53, 67, 75, 61, 70, 81, 76, 79, 75, 76, 58, 31\}$  according to the method:

**bandwidth =  $\lambda$  time the sample standard deviation of data,**  
for the two values  $\lambda = 0.5$  and  $\lambda = 0.2$ .

Sample standard deviation of a list of numbers is defined on pg. 71. It may be computed:

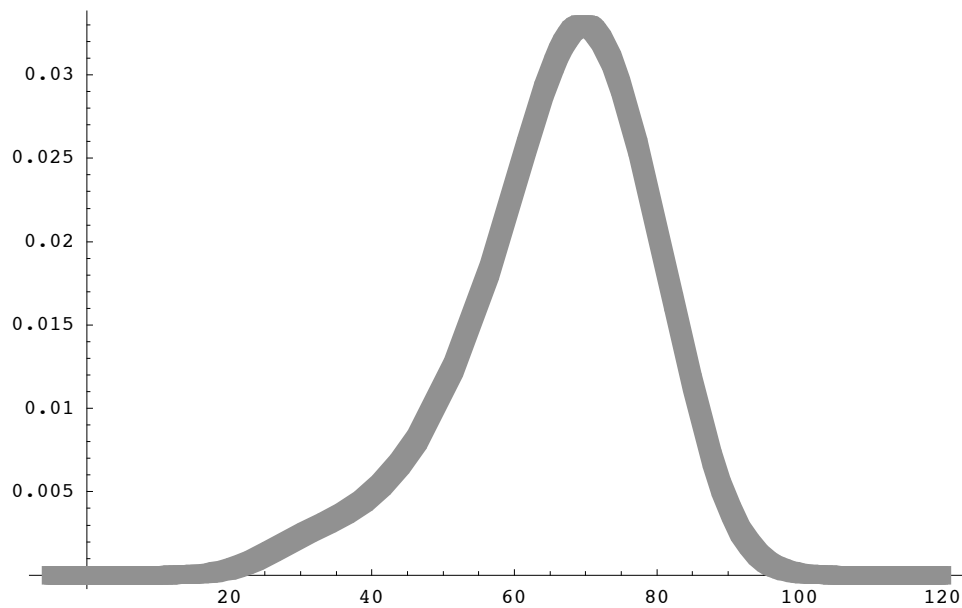
```
sd[{84,49,61,40,83,67,45,66,70,69,80,58,68,60,67,72,73,70,57,63,70,78,52,67,  
, 53,67,75,61,70,81,76,79,75,76,58,31}]
```

which returns sample standard deviation 11.9888 (just below).

```
sd[{84, 49, 61, 40, 83, 67, 45, 66, 70, 69, 80, 58, 68, 60, 67, 72, 73,  
70, 57, 63, 70, 78, 52, 67, 53, 67, 75, 61, 70, 81, 76, 79, 75, 76, 58, 31}]
```

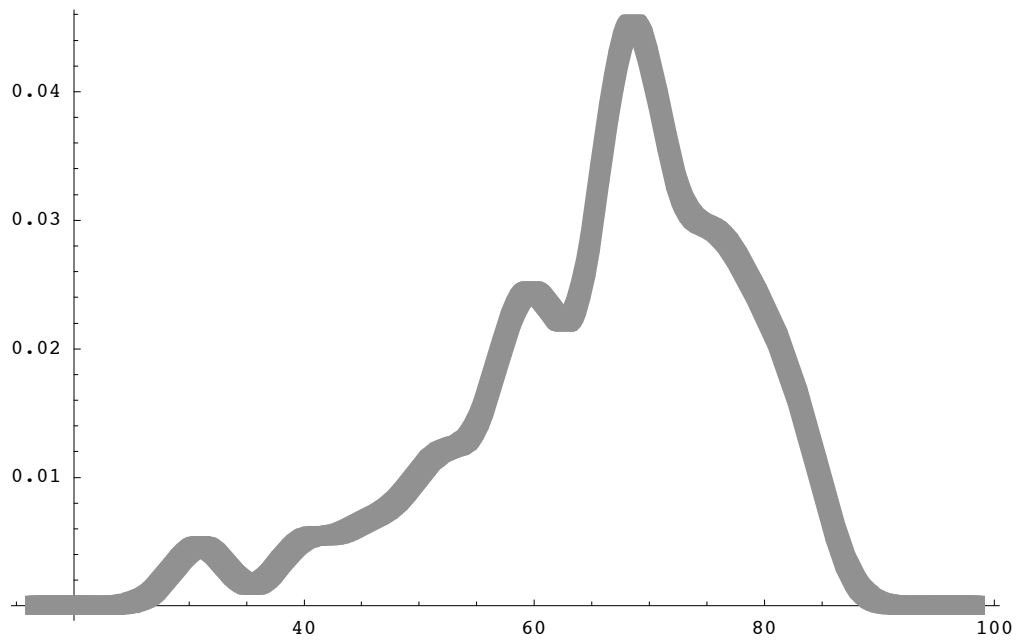
```
11.9888
```

```
smooth[{84, 49, 61, 40, 83, 67, 45, 66, 70, 69, 80, 58, 68, 60, 67, 72, 73, 70, 57,  
63, 70, 78, 52, 67, 53, 67, 75, 61, 70, 81, 76, 79, 75, 76, 58, 31}, .5 11.99]
```



- Graphics -

```
smooth[{84, 49, 61, 40, 83, 67, 45, 66, 70, 69, 80, 58, 68, 60, 67, 72, 73, 70, 57,
        63, 70, 78, 52, 67, 53, 67, 75, 61, 70, 81, 76, 79, 75, 76, 58, 31}, .2 11.99]
```

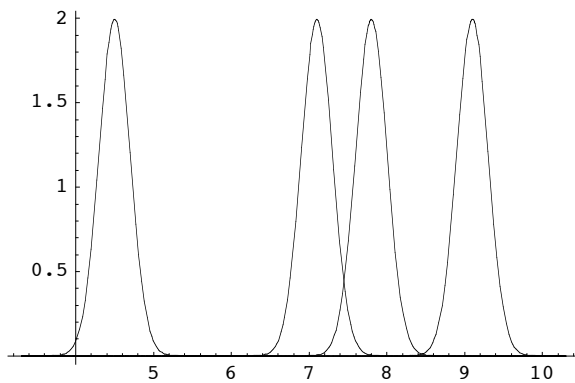


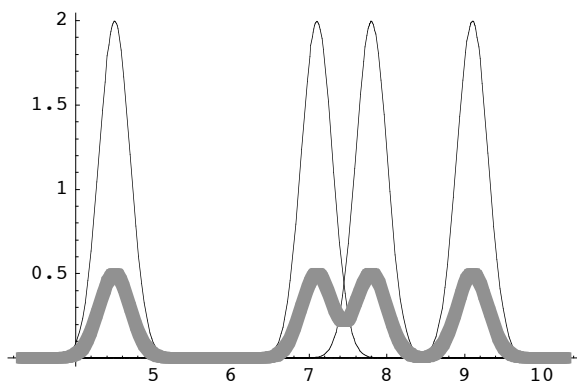
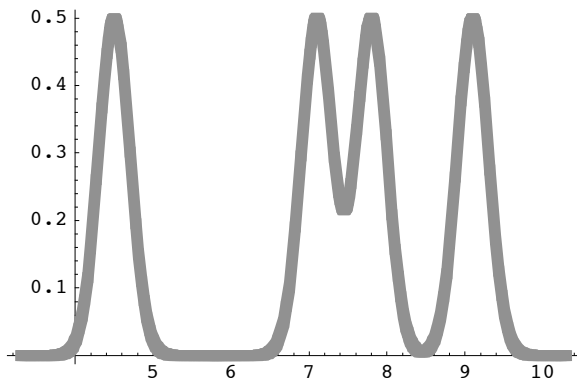
- Graphics -

The figures just above are indeed those of Figure 1.13.pg. 335.

above are Figure figures indeed just of The those 1.13.pg.335.

```
smooth2[{4.5, 7.1, 7.8, 9.1}, 0.2]
```





- Graphics -

```
R[{{1, 2}, {1, 3}, {1, 6}}, {9, 7, 5}]
```

```
0.960769
```

```
r[{{2, 3, 6}, {9, 7, 5}]
```

```
-0.960769
```

```
betahat[{{1, 2}, {1, 3}, {1, 6}}, {9, 7, 5}]
```

```
{ $\frac{135}{13}$ ,  $-\frac{12}{13}$ }
```

```
resid[{{1, 2}, {1, 3}, {1, 6}}, {9, 7, 5}]
```

```
{ $\frac{6}{13}$ ,  $-\frac{8}{13}$ ,  $\frac{2}{13}$ }
```